



# An ECCOMAS Advanced Course on Computational Structural Dynamics

Institute of Thermomechanics  
Czech Academy of Sciences

and

Faculty of Civil Engineering,  
Czech Technical University  
in Prague

Prague  
Czech Republic

**June 4-8, 2018**

## Lecturers

**Prof. K.C. Park**

University of Colorado,  
Boulder, USA

**Prof. Alain Combescure**

Institut National des Sciences  
Appliquées, Lyon, France

**Dr. Jiří Plešek**

Institute of Thermomechanics,  
Prague, Czech Republic

**Prof. Jaroslav Kruis**

Czech Technical University in Prague,  
Czech Republic

**Prof. José González**

Universidad de Sevilla, Spain

**Prof. Alexander Popp**

Bundeswehr University Munich,  
Germany

**Dr. Jin-Gyun Kim**

Institute of Machinery and Materials,  
Korea

**Dr. Anton Tkachuk**

University of Stuttgart, Germany

**Dr. Radek Kolman**

Institute of Thermomechanics,  
Prague, Czech Republic

## Topics:

The course covers topics relating to modern and recent numerical methods in *computational structural dynamics*, finite element method in linear and nonlinear dynamic cases, wave propagation in solids and its numerical solution, numerical methods in dynamic contact problems, buckling analysis, modern methods for direct time integration and partitioned analysis, modal and spectral analysis, coupled problems (e.g. fluid-structure interaction), reduction modelling in dynamics and many others.

## The short course is organized under

- European Community on Computational Methods in Applied Sciences
- Central European Association for Computational Mechanics
- Czech Society for Mechanics
- Academy of Sciences of the Czech Republic
- Institute of Thermomechanics, CAS
- Centre of Excellence for Nonlinear Dynamic Behaviour of Advanced Materials in Engineering
- Faculty of Civil Engineering, Czech Technical University in Prague

## Course schedule:

9.00 -10.00	Lecture
10.00-10.20	Coffee break
10.20-11.20	Lecture
11.20-11.40	Coffee break
11.40-12.40	Lecture
12.40-14.30	Lunch
14.30-15.30	Lecture
15.30-15.50	Coffee break
15.50-16.50	Lecture
16.50-17.15	Open discussion

**Venue:** Faculty of Civil Engineering,  
Czech Technical University in Prague,  
Thákurova 7, 166 29 Prague 6

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## Course fee: Early payment up to March 15, 2018:

300 €	for 30 students and Ph.D. students from abroad (confirmation needed, contact of organizers is needed)
500 €	for students and Ph.D. students
600 €	for post-docs and junior and senior researchers
700€	for industry and private sector

## Short Course Program:

### Monday

#### 1. Basics of dynamics and introduction with motivation (K.C. Park)

Introduction of the course  
Historical background of dynamics  
Newtonian, Lagrangian and Hamiltonian mechanics

#### 2. Continuum mechanics I (J. Plešek)

Kinematics of deformation  
Strains and stresses  
Governing equations, Strong form

#### 3. Continuum mechanics II (J. Plešek)

Constitutive equations for small strains - elasticity, hyper-elasticity, plasticity  
Numerical integration of constitutive equations

#### 4. Continuum mechanics III (A. Tkachuk)

Variational formulations in dynamics  
Mixed formulations, Tonti diagram,  
Hamilton's principle, Weak forms

#### 5. Dynamics of multibody systems (J. Kim)

Governing equations, Constrains  
Lagrange equations and Lagrange multipliers  
Numerical methods in multibody dynamics

### Tuesday

#### 6. Finite element method I - Basics (J. Gonzalez)

Principle of virtual work  
Finite Element Formulation  
Assembly of global matrices  
Convergence properties

#### 7. Finite element method II (J. Gonzalez)

Shape functions and higher order FEM  
Isoparametric formulation  
Numerical integration  
Hybrid and mixed formulation, inf-sup condition

#### 8. Finite element method III - Mass matrices (A. Tkachuk)

Properties of mass matrix  
Consistent and lumped mass matrices  
Higher-order mass matrix  
Direct inversion of mass matrix

#### 9. Finite element method IV (J. Gonzalez)

Implementation of FE codes for linear dynamics (Matlab)

### 10. Poster section of participants

### Wednesday

#### 11. Finite element method V – Beams and Plates (A. Combescure)

Basics of beam theory – Euler-Bernoulli and Timoshenko theory  
Basics of plate theory - Kirchoff-Love and Mindlin theory  
FEM for beams and plates

#### 12. Finite element method VI – Shells (A. Combescure)

Basics of shell theory  
FEM shell models  
Shells in dynamics

#### 13. Finite element method VII (A. Tkachuk)

Locking phenomena and hourglass effect  
Assumed strain, enhanced strain FEM,  
B-bar formulation  
Reduced integration and stabilization

#### 14. Finite element method VIII– Linear Solvers (J. Kruijs)

Linear solvers in FEM  
Matrix factorization

Sparse solvers, Krylov methods  
(especially conjugate gradient method)

#### 15. Finite element method IX (J. Kruijs)

FEM in vibration problems  
Spectral and modal analysis  
Numerical methods for eigen-value problem (subspace iteration, etc)  
Convergence of FEM in eigen-value problem  
Dynamic steady state response

### Thursday

#### 16. Finite element method X (A. Popp)

Basics of nonlinear continuum mechanics, FEM for nonlinear problems,  
Total Lagrangian formulation, Nonlinear solvers - Newton-Raphson method

#### 17. Finite element method XI - Direct time integration in dynamics (R. Kolman)

FEM in dynamics, formulation of dynamic problems  
Introduction into direct time integration  
Basic methods (Newmark method and central difference method)  
Solving of nonlinear time-depend problems  
Time step size estimates, mass scaling

#### 18. Buckling phenomena (A. Combescure)

Linear theory of stability  
Solution methods, path following techniques  
Identification of critical points  
Pre-buckling analysis and nonlinear stability analysis

#### 19. Wave propagation (R. Kolman)

Theory of wave propagation in elastic solids, Wave speeds in solids  
Dispersion and frequency analysis of FEM,

#### 20. Partitioned analysis (K.C. Park)

Theory of Lagrange multipliers  
Basic theory of partitioned analysis  
Equations of motion for partitioned systems, Domain decomposition methods and FETI

### Friday

#### 21. Model reduction in dynamics (J. Kim)

Variational analysis of dynamic sub-structuring, Hurty and Craig-Bampton methods, dynamic reduction, mode selection, error estimation,

#### 22. Contact problems I (A. Popp)

Basics of contact mechanics, FEM for contact problems  
Penalty, Lagrange multiplier and Augmented Lagrangian methods

#### 23. Contact problems II (A. Popp)

Modeling of friction  
Advanced discretization techniques and solution algorithms  
Mortar methods, Semi-smooth Newton methods

#### 24. Coupled problems – Fluid-structures interactions (K.C. Park)

Variational formulation  
Methods of discretizations  
Staggered analysis

#### 25. Closing and discussion