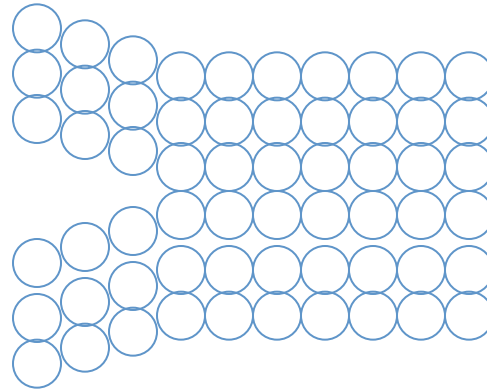


Griffith picture (1921)

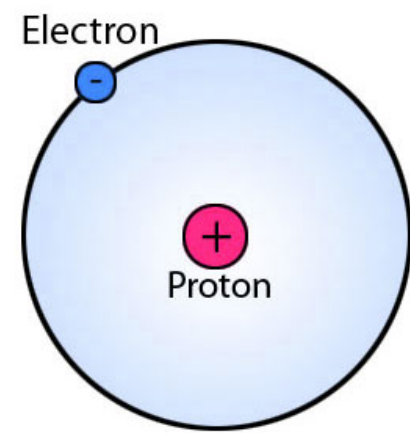
Rupture of **silica**



$$\text{fracture energy} = \frac{\text{covalent energy of a single layer of atoms}}{\text{area}}$$

$$\Gamma \approx 1\text{J/m}^2$$

Chemical bond



Quantum mechanics
Schrodinger (1926)

$$\left[\frac{\hbar^2}{2m} \nabla^2 + \frac{e^2}{4\pi\epsilon_0 r} + E \right] \Phi = 0$$

Length

$$a = \frac{4\pi\epsilon_0 \hbar^2}{me^2} = 0.5 \times 10^{-10} \text{ m}$$

Energy

$$E = \frac{me^4}{2(4\pi\epsilon_0 \hbar)^2} = 13.6 \text{ eV} = 25.8 \times 10^{-19} \text{ J}$$

In the above, the groups of physical quantities are obtained from dimensional considerations of the differential equation, and the numerical coefficients are for the hydrogen atom. Hydrogen atom is particularly small and the energy is particularly large. A representative atomic size is $a \sim 3 \times 10^{-10} \text{ m}$. A representative energy of a covalent bond is $E \sim 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$.

Surface energy

$$\gamma \sim E / a^2 \sim 1 \text{ J/m}^2$$