

EM 388 F - Fracture Mechanics [Dr. Huang]

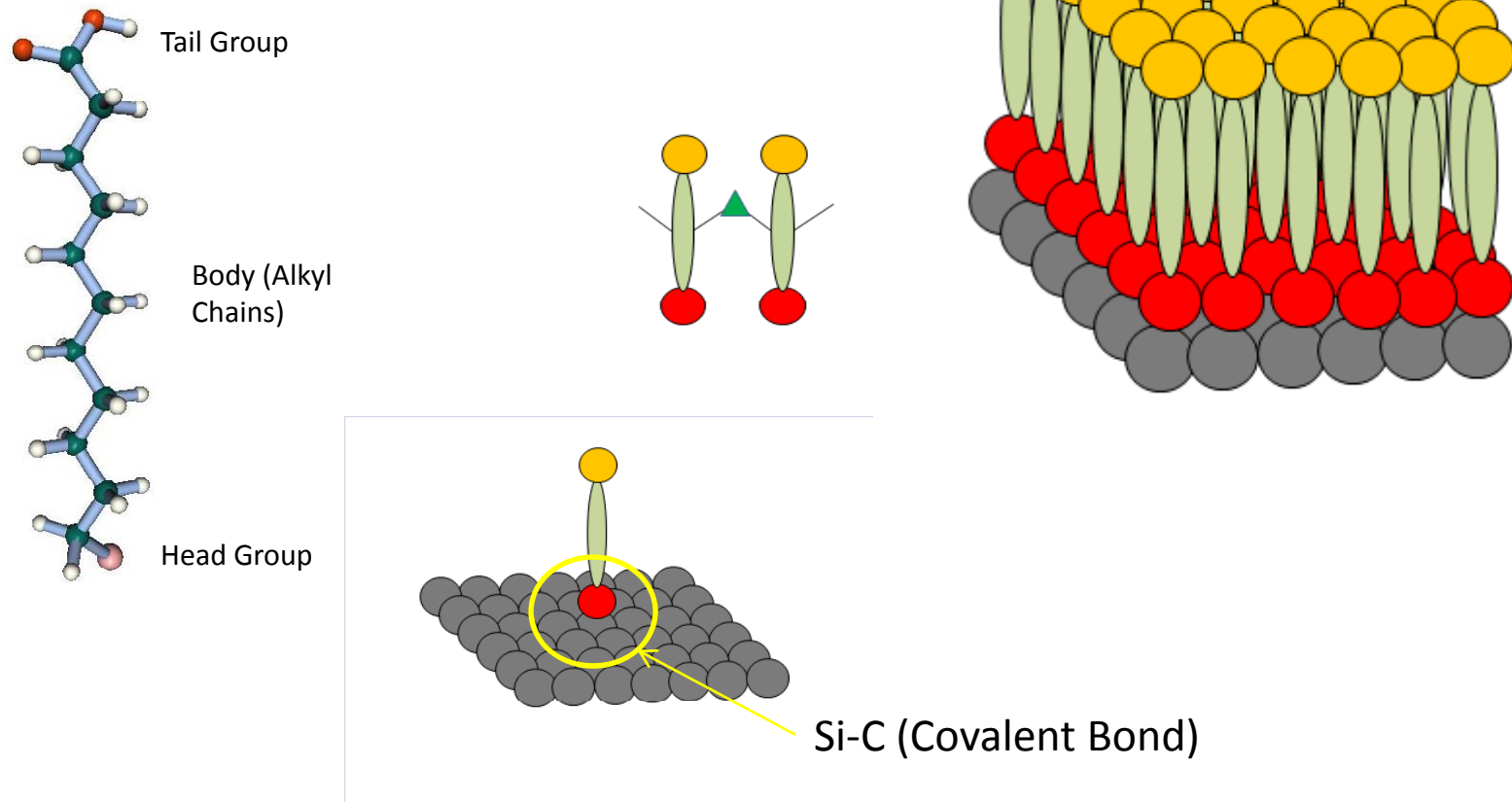
Final Project - Study of Mode I Fracture of Self Assembled Monolayer  
with ABAQUS

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## Introduction 1/14

### What is Self Assembled Monolayers?



SAMs can be sticky or non-sticky by altering a tail group.  
In this study, consider SAM as an ultra thin layer of adhesive.

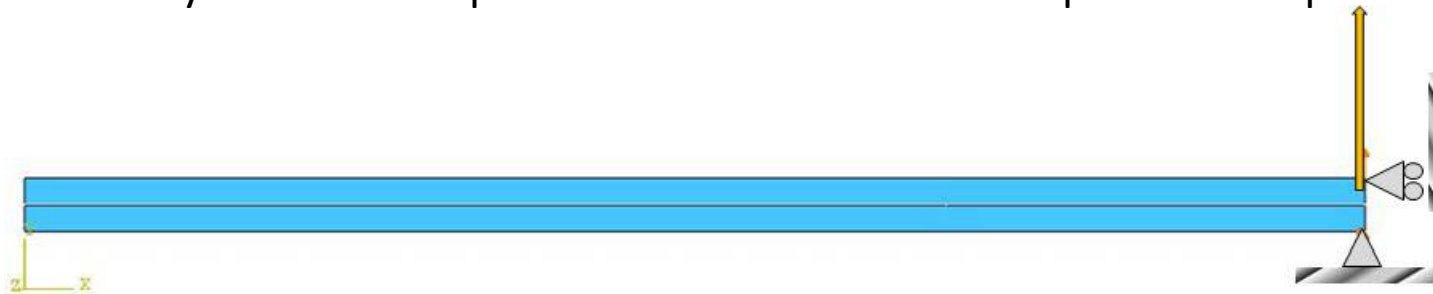
Reference: A. Ulman. Formation and Structure of Self-Assemble Monolayers. *Chemical Reviews* 96: 1533-1554, New York (1996)

## Introduction 2/14

When DCB specimen is subjected to ramp input in a Mode I manner, available data are reaction load (P) and displacement (delta) at the location here loading is applied.

### Objective of Study:

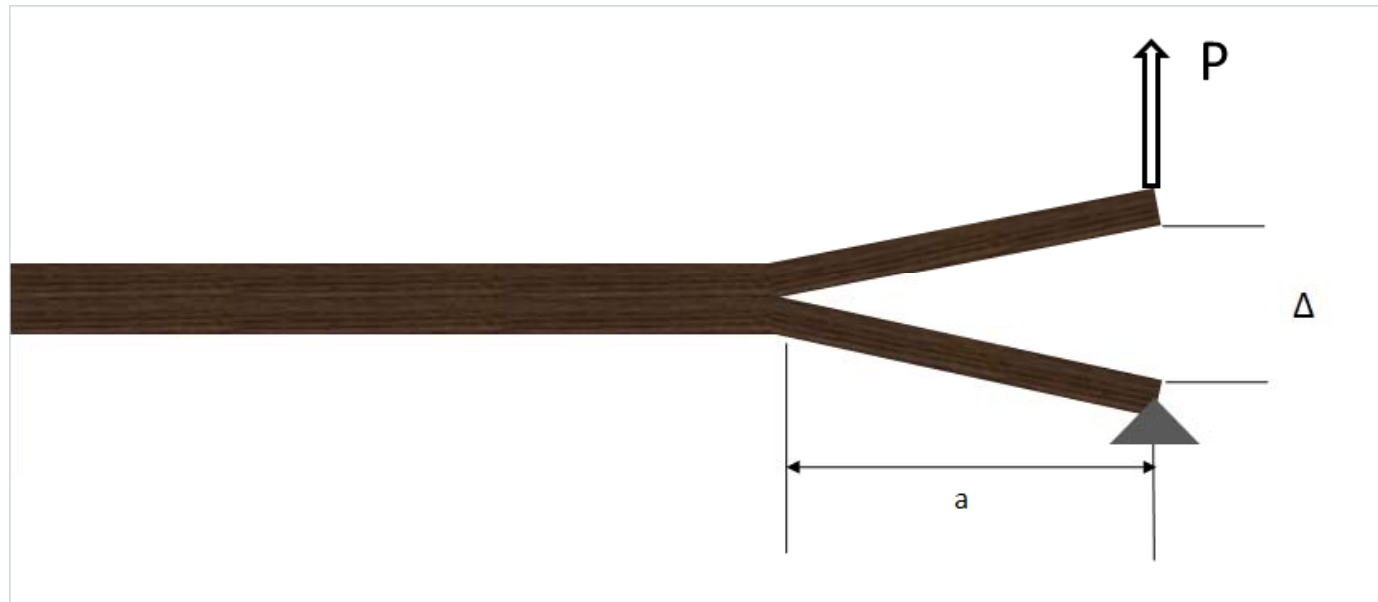
1. Learn ABAQUS program (exp. Cohesive element)
2. Study P vs delta response from various traction separation shapes



| Material Property | Input is in yellow |     |           |          |
|-------------------|--------------------|-----|-----------|----------|
|                   | m base unit        |     | mm Unit   |          |
|                   | (unit)             |     | (unit)    |          |
| L                 | 1.60E-02           | m   | 16        | mm       |
| b                 | 5.00E-03           | m   | 5         | mm       |
| h                 | 3.20E-04           | m   | 0.32      | mm       |
| E                 | 1.69E+11           | Pa  | 1.69E+05  | N/(mm^2) |
| nu                | 3.00E-01           |     | 0.22      | N/A      |
|                   |                    |     |           |          |
| Test Property     |                    |     |           |          |
| BCs               | Bottom/Up          |     | Bottom/Up |          |
| Loading rate      | 1.00E-05           | m/s | 1.00E-02  | mm/ sec  |

Substrate: Silicon(111)

## Theory 3/14 – LEFM Energy Method



Energy Release Rate

$$G_{tip} = \frac{\eta P^2 a^2}{E b I}$$

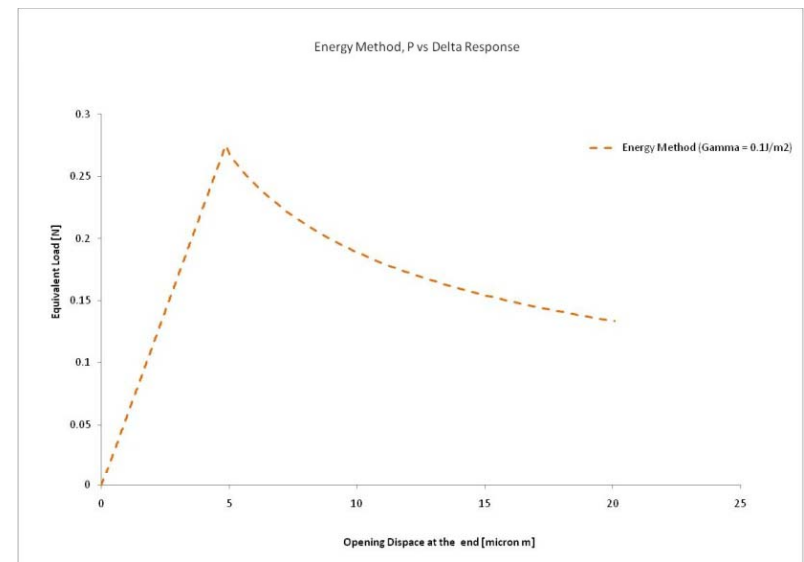
for plane strain,

$$\eta = 1 - \nu^2$$

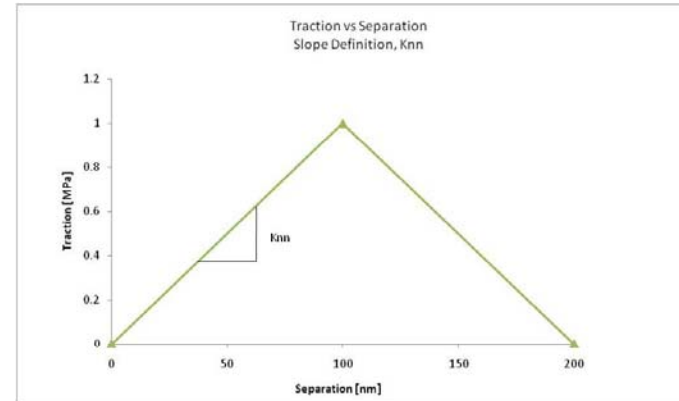
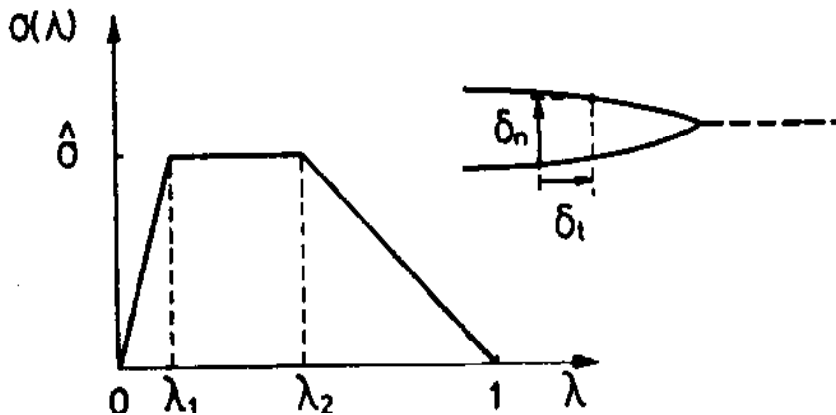
Tip Deflection

$$\Delta = 2 \times \delta$$

$$\delta = \eta \frac{P a^3}{3 E I}$$



## Theory 4/14 – Traction Separation



- In 1960's, Dugdale, Bilby, Cottrell, established the concept of traction separation properties of interface fracture driven from atomic separation to void growth (Bao and Suo) +
- When adhesive is thin compared to thickness of a substrate, mode mixity is almost zero (Gdoutos) ++

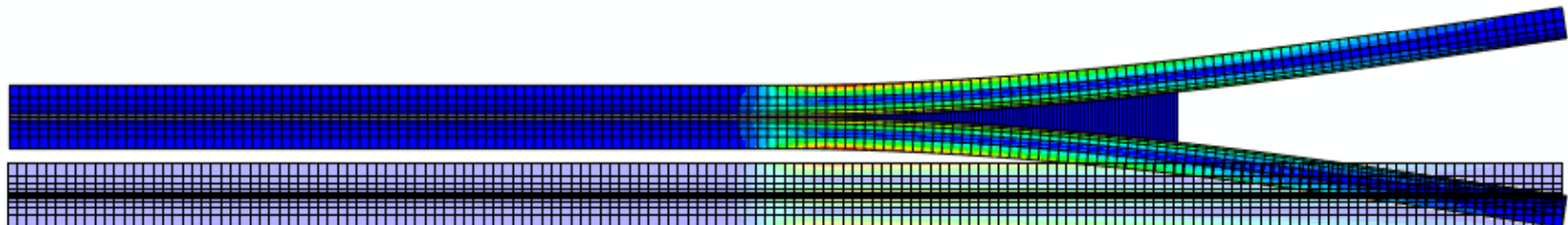
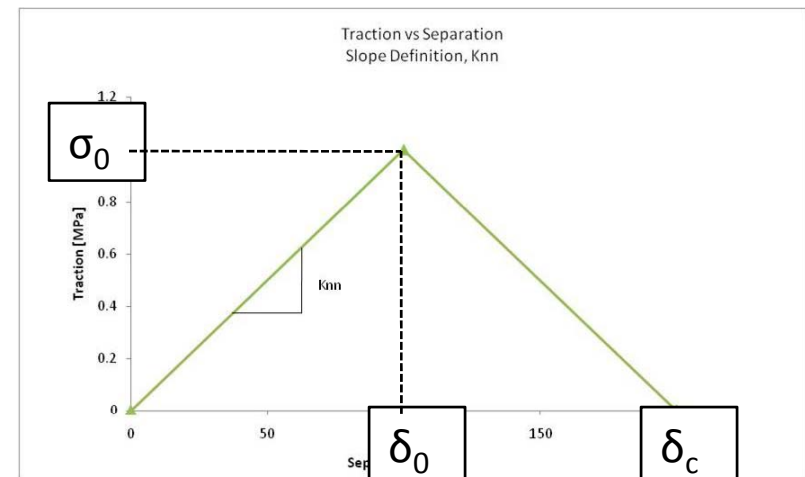
### Referece

- + G. Bao. Z Suo. Remarks on crack-bridging concepts. Appl. Mech. Rev. vol. 45. (1992)
- ++ E. Gdoutos. Fracture Mechanics 2<sup>nd</sup> Edition. Greece (2005)

## Case Studies 5/14

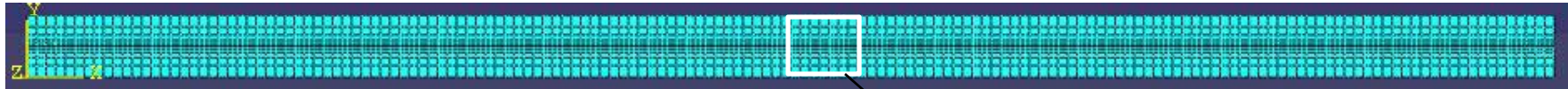
From previous work with OTS by Wang (2004), interfacial fracture energy is set as  $0.1 \text{ J/m}^2$  (i.e. area underneath of Traction Separation curve).

- \* *Case 1 [const. fracture energy]*  
Keep  $\sigma_0$  and  $\delta_c$  constant, vary  $\delta_0$
- \* *Case 2 [const. Knn, diff energy]*  
Keep Knn and  $\delta_c$  constant, vary  $\sigma_0$
- \* *Case 3 [const. fracture energy]*  
Keep  $\Gamma_0$  constant, vary  $\sigma_0$ ,  $\delta_0$ , and  $\delta_c$



# ABAQUS Model 6/14

## Parametric Study of Cohesive Element in Mode I - Meshes



Si wafer: Plain Strain Condition

Element Type: **CPE8R**

An 8-node biquadratic plane strain quadrilateral, reduced integration.

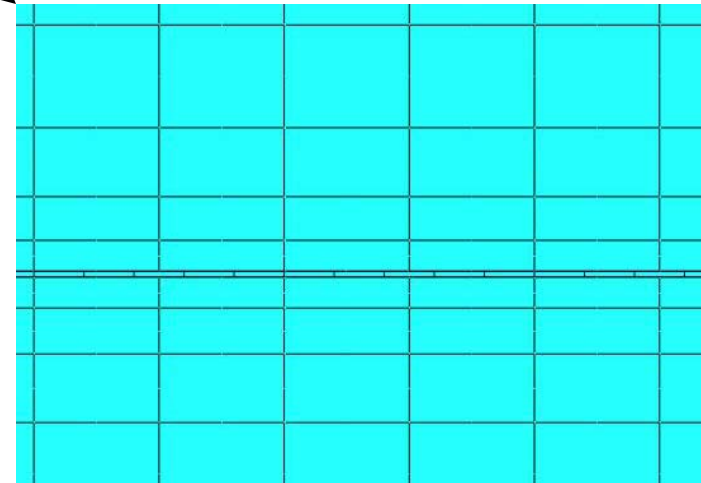
SAM: Plain Strain Condition

Element Type: **COH2D4**

A 4-node two-dimensional cohesive element.

Thickness: Default (i.e. 1)

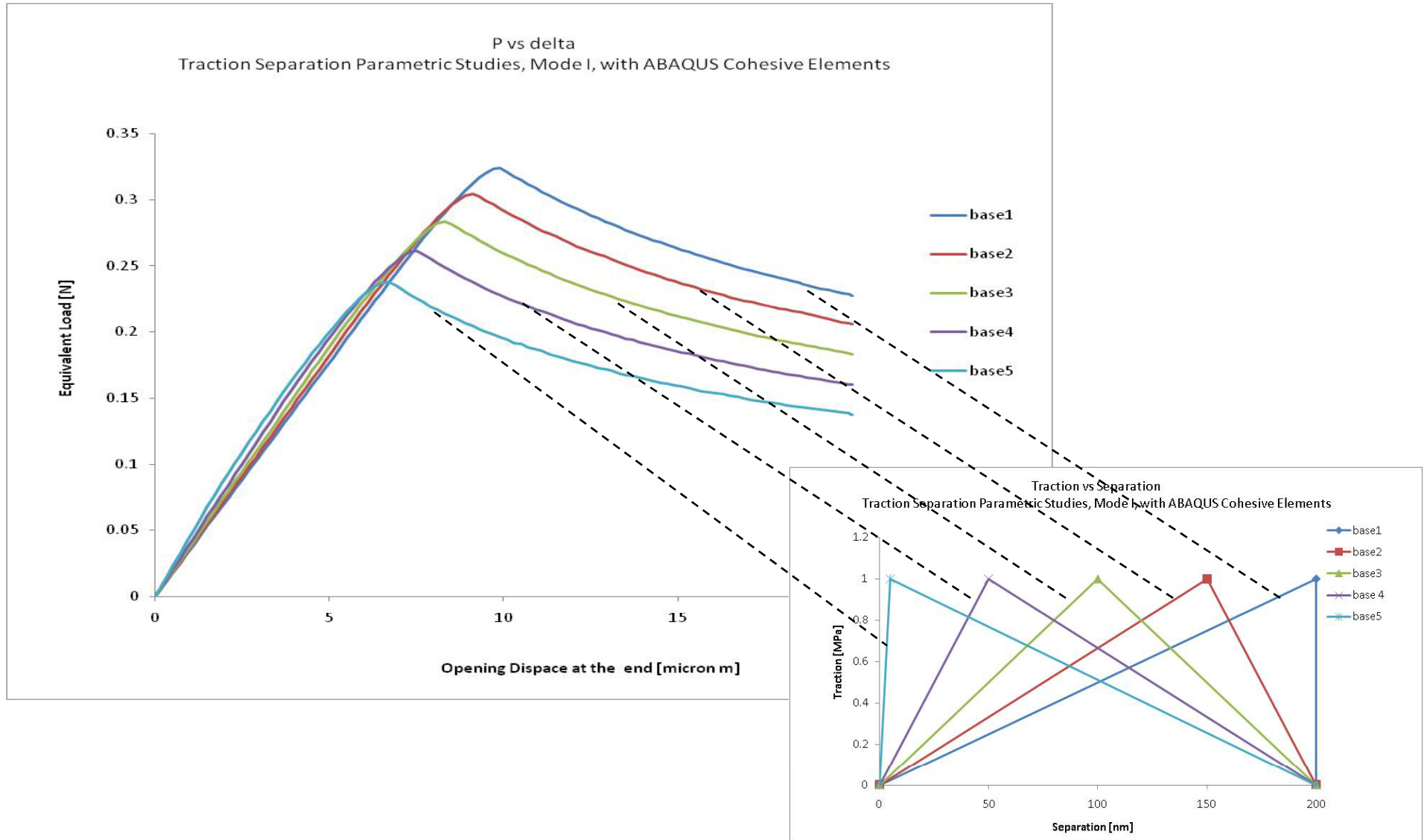
Maxe damage criterion



|                           |       |
|---------------------------|-------|
| Total number of elements  | 1900  |
| number of nodes           | 6064  |
| total number of variables | 12128 |

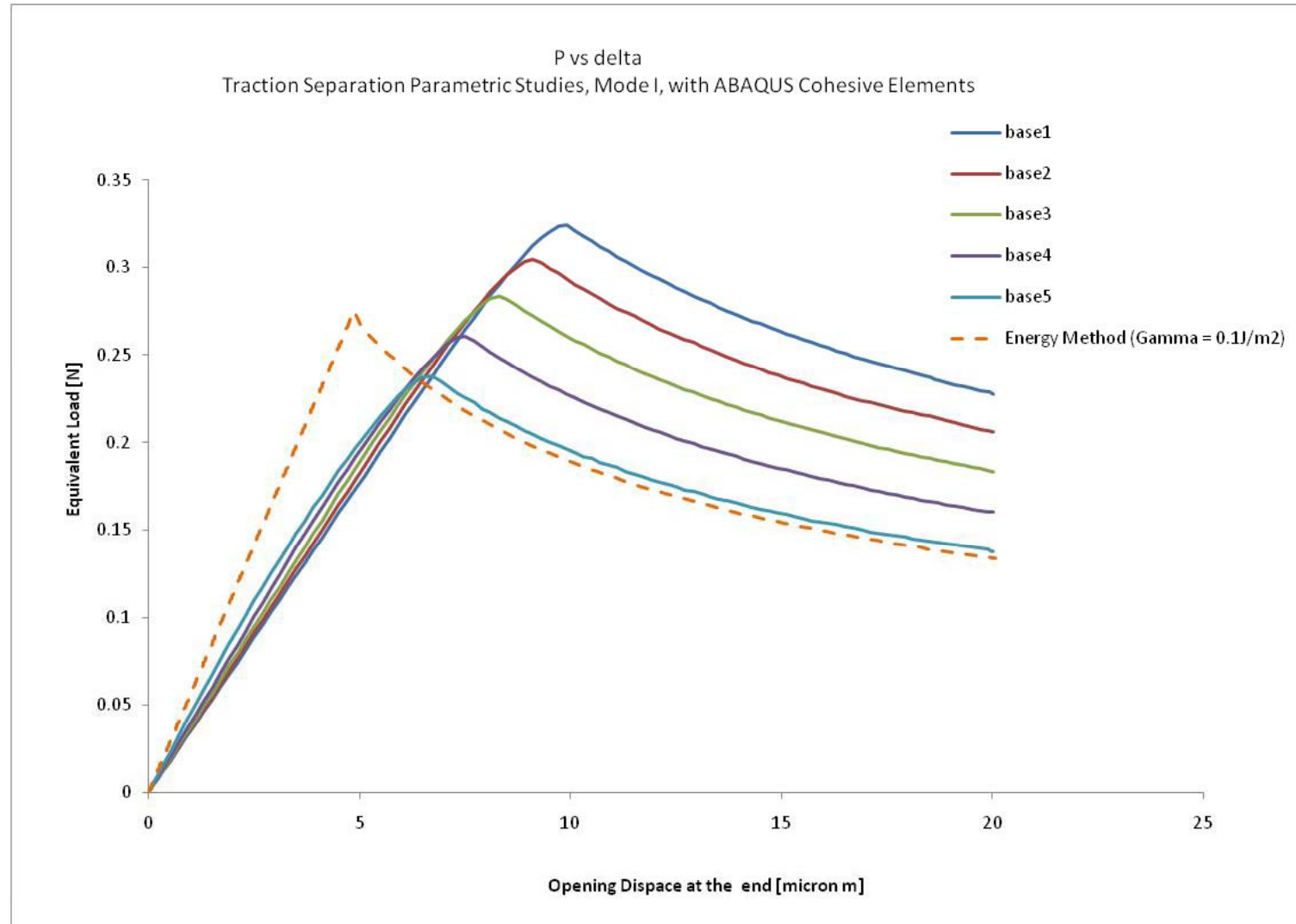
# Case 1 Results 7/14

## Case 1 Parametric Study of Cohesive Element in Mode I - Results



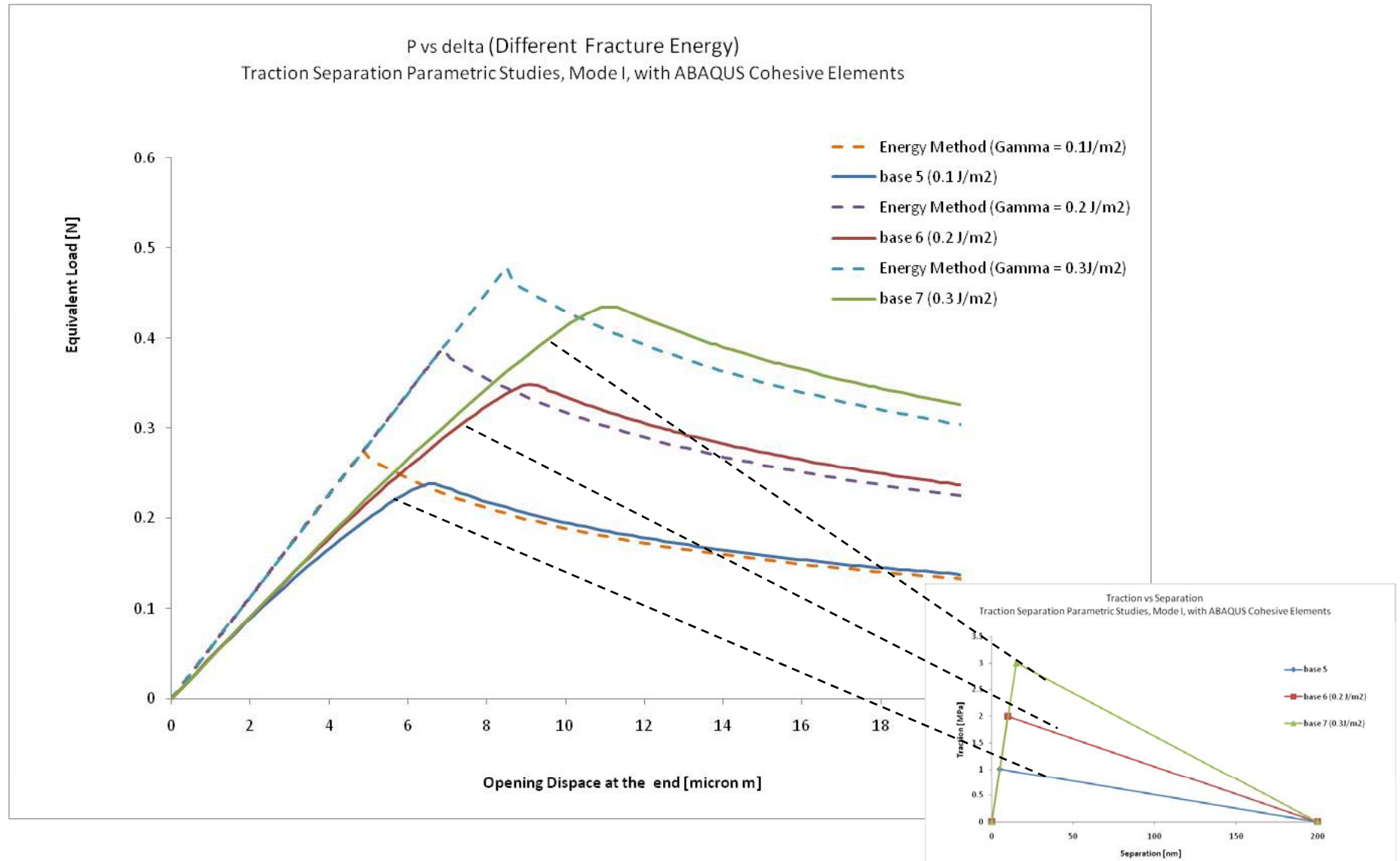


## Case 1 Results 8/14



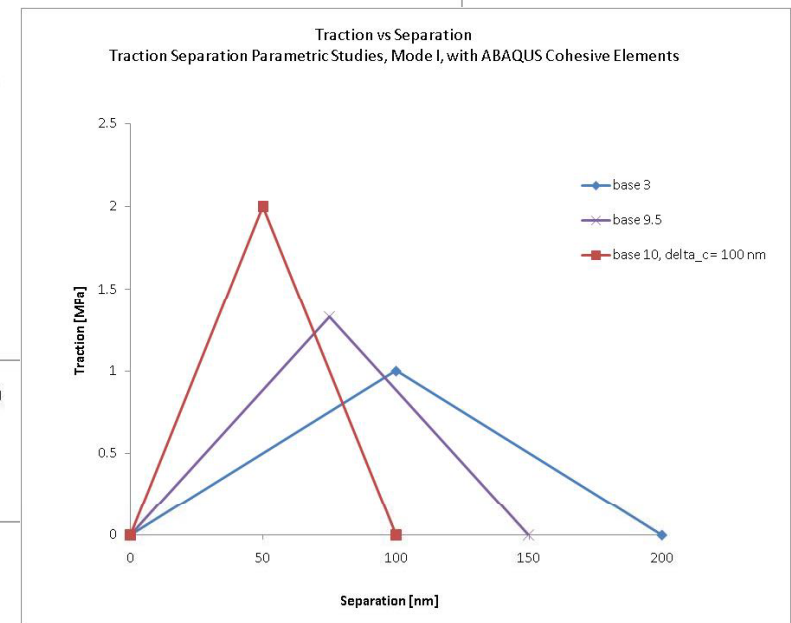
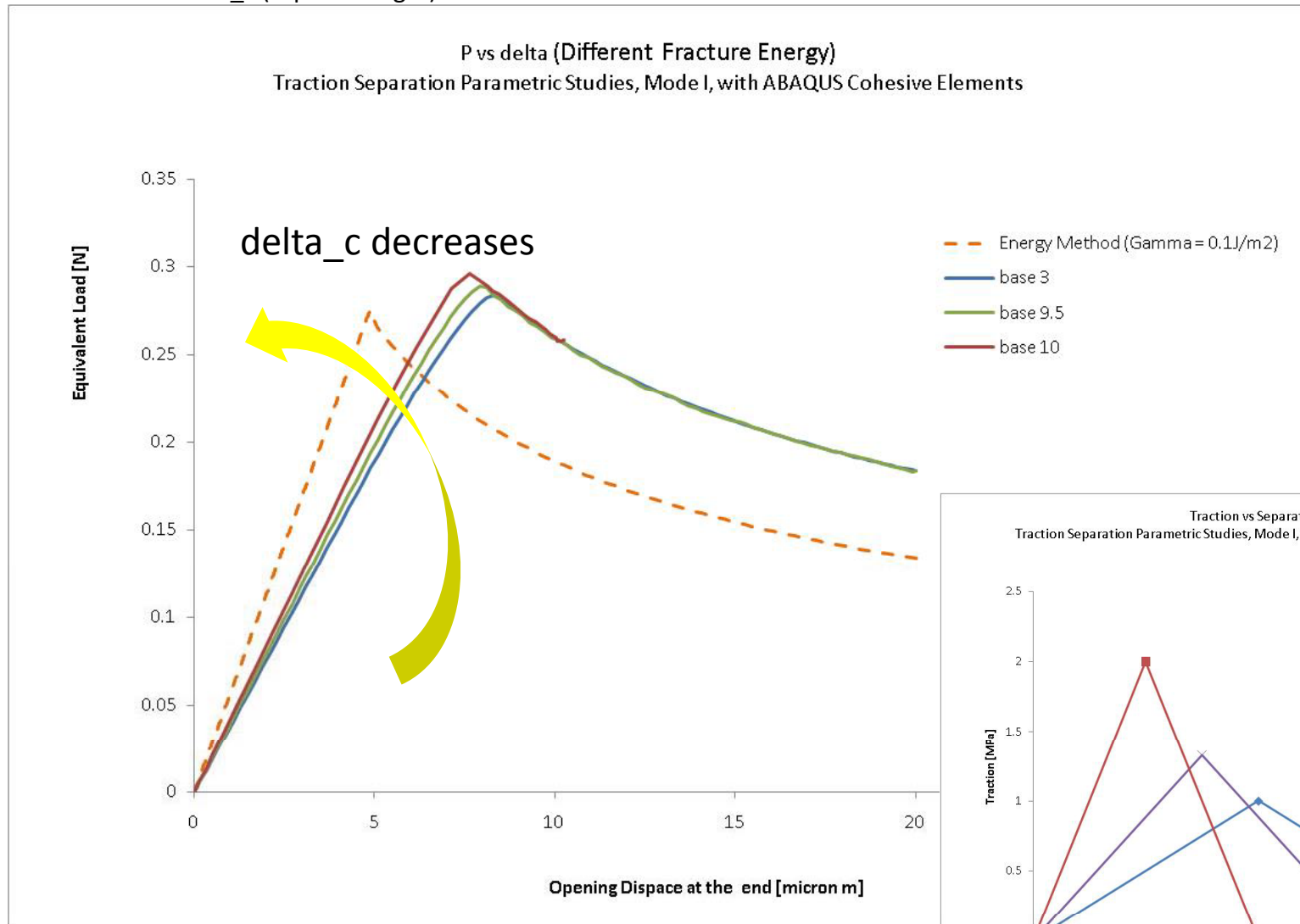
## Case 2 Results 9/14

### Case 2 Increase Interfacial Fracture Energy



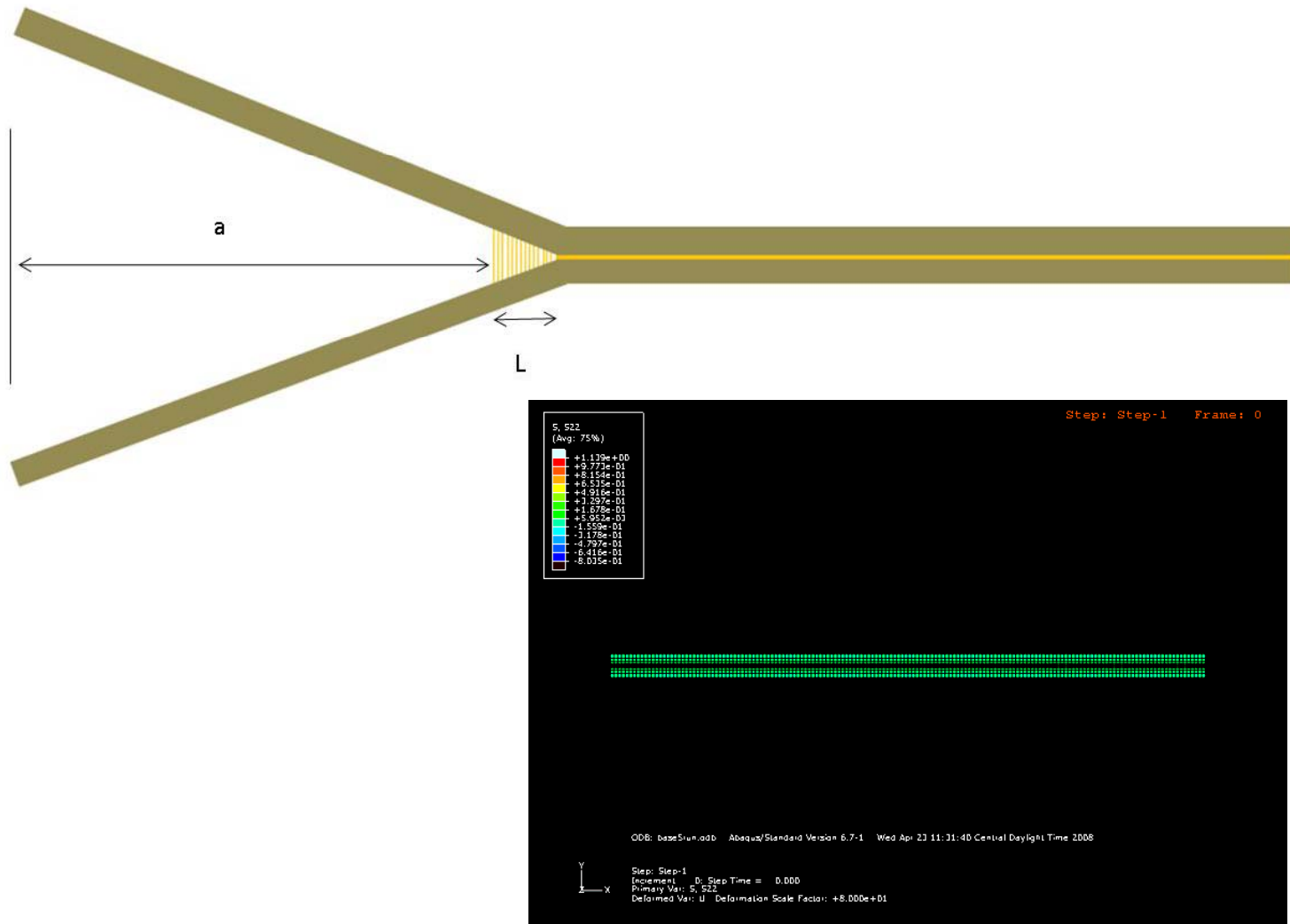
## Case3 Results 10/14

Case 3 Make  $\delta_c$  (rupture length) shorter

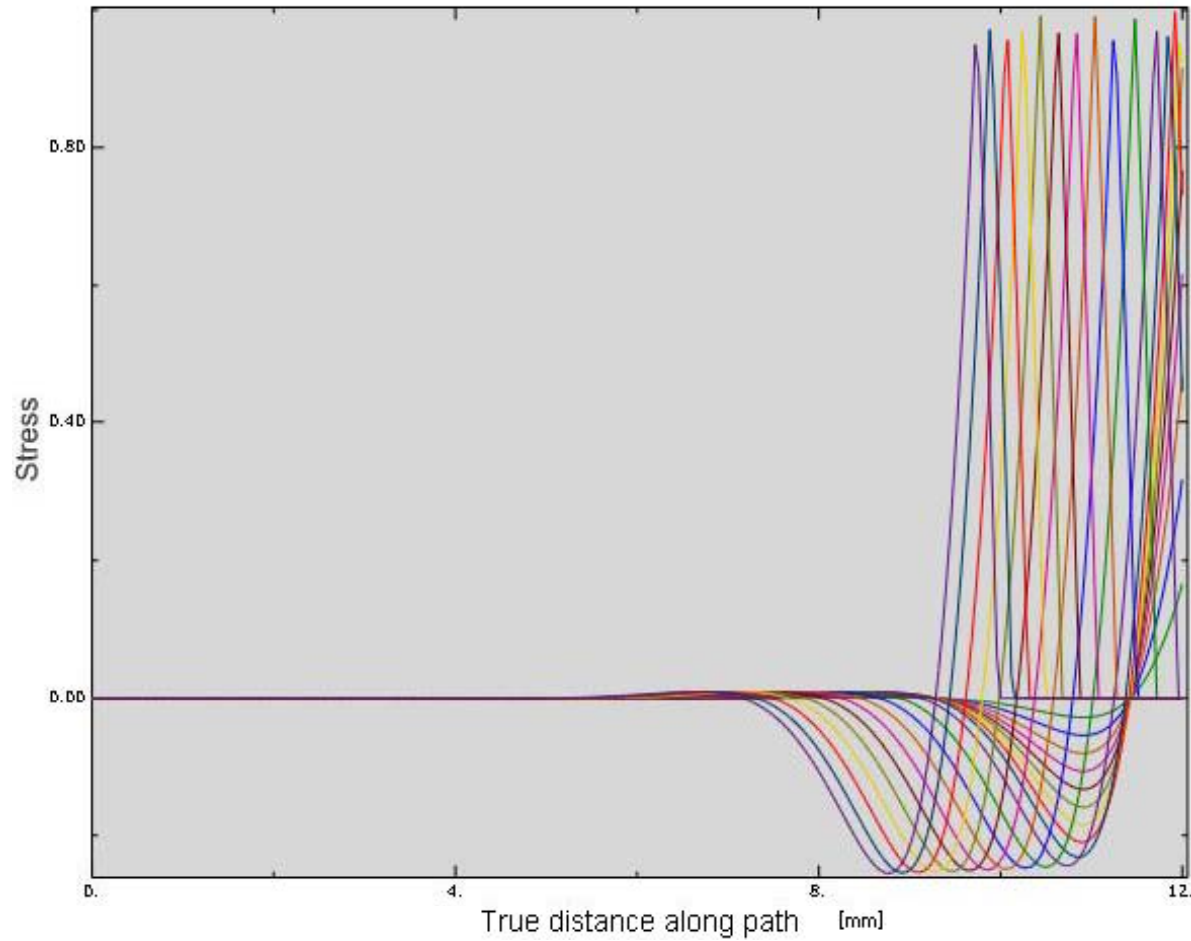


## Crack Propagation Results 11/14

How does crack propagate?

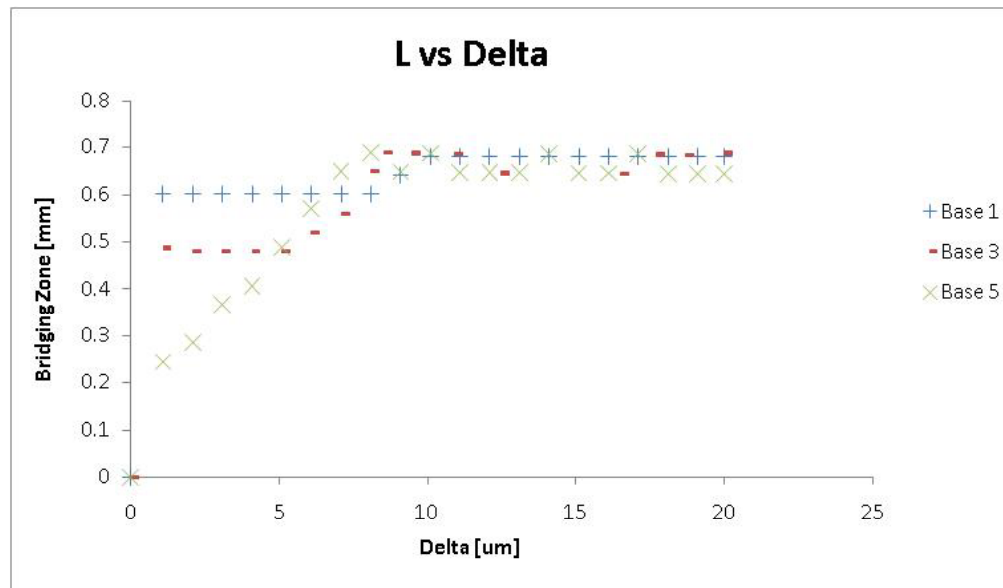
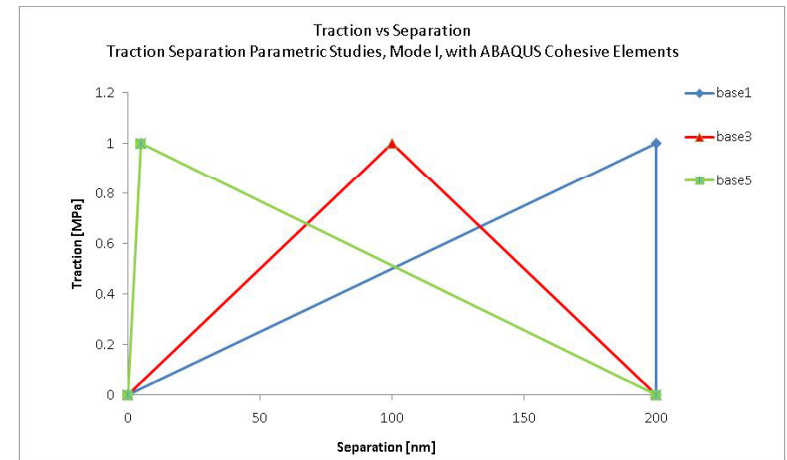
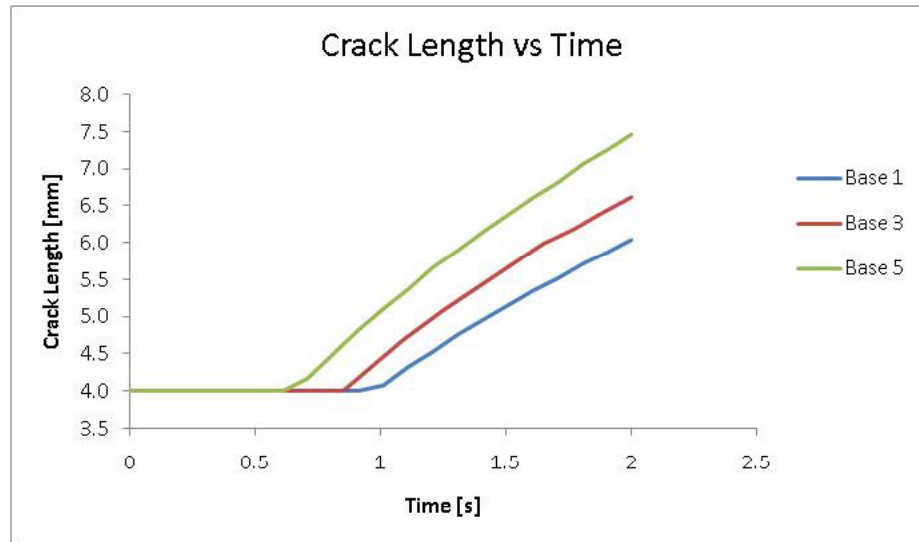


## Crack Propagation Results 12/14



Method: Define a path along cohesive element. Then, take  $\sigma_{22}$  data for each 0.1 sec. Recall that input (disp) was 0.01 mm/sec.

## Crack Propagation Results 13/14



## Conclusion14/14

Case 1: As slope of T-S increases (as  $\delta_0$  decreases), P required to propagate the crack decreased.

Case 2: As interfacial fracture energy increases, P required to propagate the crack increased.

Case 3: As separation length shortens ( as  $\delta_c$  decreases), slope of P vs delta curve became higher.

Crack Propagation: Although the interfacial fracture energy remains constant, crack propagation depended on the slope of T-S property. However, Lss length was identical to any slope with the same interfacial fracture energy.

Lss was about 0.68 mm, which is larger than thickness of Si substrate. Thus, this problem should be considered as “Large Scale Bridging.”

Future Works: Study mix-mode (Mode I and Mode II) conditions